

## MATHS TEST

Time allowed: 45 min

### Question 1

Prove the identity;

$$\left( \frac{a + \sqrt{a^2 - 1}}{a - \sqrt{a^2 - 1}} + \frac{1 - \frac{a}{\sqrt{a^2 - 1}}}{1 + \frac{a}{\sqrt{a^2 - 1}}} \right) \div \left( \frac{\sqrt{a - \frac{1}{a}}}{\sqrt{\frac{1}{a}}} \right) = 4a$$

### Question 2

Solve the simultaneous equations:

$$\begin{cases} 2x - y = 1 \\ 2x^2 - y^2 + x + y = -11 \end{cases}$$

### Question 3

Find all the values of  $a$  such that the equation has exactly one real root:

$$x^2 + 2ax + 12 - a = 0$$

### Question 4

Sketch the graph of the function  $y = -2x^2 + 3x + 2$  where  $x \in \left[-\frac{1}{2}; 2\right]$ .